

- **The source-filter model of vowel acoustics**
- **The glottal source**
- **Modeling schwa**

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*Background reading:*

- *AAP* Ch 2, sec 2.1 and 2.4 (review)

# 0. Today's plan

- Review/check-in: Tube resonances
- Overview of the source-filter model
- The glottal-source wave
- The vocal-tract filter
- Deriving the vocal-tract filter for [ə]
- Putting source and filter together: [ə]
- Terms and abbreviations for frequencies

# 0. Review: Tube resonances

- Last week in class:

How do we get from tube length to resonance frequencies?

- Lab #3:

How do we get from resonance frequencies to tube length?

# 1. Overview of the source-filter model

- How do you get a trumpet to play a note?

# 1. Overview of the source-filter model

- To play a trumpet, you “buzz” your lips
  - This creates a **sound source** at one end of the trumpet (disturbance in the medium!)
- But what we *hear* is a trumpet note, not a buzz:  
The trumpet acts as a **filter**
  - It **changes the shape** ( → the **sound quality**) of the **complex wave** produced by the sound source
  - It does this by **suppressing** (reducing the amplitude of) some of the source wave’s **components** and **amplifying** (increasing the amplitude of) others

# 1. Overview of the source-filter model

- In much the same way, when we produce a **voiced speech sound** such as a **vowel**...
  - The vocal folds **buzz** (glottal-source wave)
  - The vocal-tract tube **changes the shape** of the complex wave by **suppressing** some source **components** and **amplifying** others

- The **source-filter model** of the vocal tract
  - Sound **source**: the **vibrating vocal folds**
  - **Filter**: the vocal tract as a **tube**  
(or a series of tubes)

## 2. The glottal-source wave

- What is the **glottal-source wave**?
  - Also called the **voicing wave**(form) in *AAP* Ch 2
  - The sound wave produced by \_\_\_\_\_

## 2. The glottal-source wave

- What is the **glottal-source wave**?
  - Also called the **voicing wave**(form) in *AAP* Ch 2
  - The sound wave produced by **the vibration of the vocal folds**
- To actually hear this sound wave, you would have to put a microphone right above the glottis
  - The sound waves of any speech we normally hear are **further modified** by passing through the vocal tract
    - That is the **filter** part of the model!



## 2. The glottal-source wave

- In the source-filter model of vowel acoustics:  
Sound **source** = vibrating vocal folds (**voicing**, also called **phonation**)
  - The **shape** of this wave is determined by the way the vocal folds open quickly and close gradually  
→ More about this later in the semester

## 2. The glottal-source wave

- Computer-synthesized glottal-source wave:  
[\[lsrc.wav\]](#) (U Delaware Speech Research Tutorials)
- Look at the **waveform** in Praat
  - Periodic? Simple or complex? What is  $f_0$ ?

## 2. The glottal-source wave

- Computer-synthesized glottal-source wave:  
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- Look at the **waveform** in Praat
  - Periodic? Simple or complex? What is  $f_0$ ?
- Look at the **spectrum** (window length = 0.5 sec)
  - What is the lowest-frequency component?
  - How do the components' **frequencies** relate?
  - How do the components' **amplitudes** relate?
  - What is  $f_0$ ? (should get the same answer as above!)

## 2. The glottal-source wave

- Characteristics of the glottal-source wave
  - **Amplitudes** of the components gradually **decrease** (assuming modal or 'ordinary' voicing)
  - **Frequencies** of the components are **whole-number multiples** of the lowest component
- The component frequencies thus have the *same relationship* as in a node/node system
  - Careful here: The vocal folds do not actually vibrate like a string of fixed length (they open and close to emit puffs of air)

## 2. The glottal-source wave

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- Can the **frequencies** of the **components** of the glottal-source wave be manipulated by the speaker?

**Yes!**

- Each human's voice can produce a range of  $f_0$  values (or else singing would be impossible)
- Manipulating  $f_0$  means manipulating the component frequencies
  - $f_0$  is the GCD of the component frequencies
  - So in the glottal-source wave,  $f_0$  is the same as the first component frequency

## 2. The glottal-source wave

- If someone produces a vowel with  $f_0 = 250 \text{ Hz}$ , what are the frequencies of the **first five components** of the **glottal-source wave**?

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- If someone produces a vowel with  $f_0 = 250$  Hz, what are the frequencies of the **first five components** of the **glottal-source wave**?
  - $f_1$  (H1) =  $f_0 = 250$  Hz | *don't forget the first one!*
  - $f_2$  (H2) =  $2 * f_1 = 500$  Hz | *whole-number multiples*
  - $f_3$  (H3) =  $3 * f_1 = 750$  Hz
  - $f_4$  (H4) =  $4 * f_1 = 1000$  Hz
  - $f_5$  (H5) =  $5 * f_1 = 1250$  Hz
- The components of the glottal-source wave are often called **harmonics**, abbreviated **H(n)**



### 3. The vocal-tract filter

- Much like a trumpet, the vocal tract **filters** the sound energy by **suppressing** some **components** of the glottal-source wave and **amplifying** others
  - The components **amplified** by the vocal tract are those close to its **resonance frequencies**
  - The **resonance frequencies** of the vocal tract depend on its **length** and **shape**
  - The vocal tract forms different **shapes** for different **vowels** (and consonants—more on this later)
- Therefore, each different **vowel** (such as [i] vs. [a]) corresponds to a different vocal-tract **filter**

### 3. The vocal-tract filter

- So if each different **vowel** corresponds to a different vocal-tract **filter** ...

This means that each **vowel** corresponds to a different set of **amplified frequencies** (vocal-tract **resonances**)

- **These are known as the vowel's formants**

### 3. The vocal-tract filter

- Try it out: Synthesized vowels [[lii.wav](#)] | [[laa.wav](#)]  
(U Delaware Speech Research Tutorials)
- Download and open these sound files in Praat
  - What **vowels** are they? (What do you hear?)
  - Compare them to each other and to the glottal-source wave we looked at before [[lsrc.wav](#)]:
    - How do their  **$f_0$ s** compare?
    - How do their waveform **shapes** compare?
    - How do their **spectra** compare?

### 3. The vocal-tract filter

- Each vowel (such as [i] vs. [a]) corresponds to a different set of **resonance frequencies (formants)**
- The **shape of a complex wave** is determined by the frequencies **and amplitudes** of its components
  - Two different vowel categories have **differently shaped** sound waves *even when they are sung on the same pitch* (=have the same glottal-source wave)
- Waves of different shapes correspond to sounds with different **sound qualities (timbres)** — this is how different vowels differ perceptually

## 4. Deriving the vocal-tract filter for [ə]

- To analyze the acoustics of vowels, we need to understand **why** they have the resonance frequencies (formants) that they have
- The first step: What are the resonance frequencies of the **neutral vocal-tract vowel, [ə]**?
  - The vocal tract is approximately a **uniform tube** that is **closed** at one end (the glottis) and **open** at the other end (the lips)
  - The neutral vocal-tract vowel is typically represented as [ə] (schwa), but note that it doesn't sound exactly the same as English [ə] as in *sofa*

## 4. Deriving the vocal-tract filter for [ə]

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  - What do we need to know in order to find the resonance frequencies of this vowel?

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- The first step: What are the resonance frequencies of the **neutral vocal-tract vowel, [ə]**?
  - The vocal tract is approximately a **uniform tube** that is **closed** at one end (the glottis) and **open** at the other end (the lips)
  - What do we need to know in order to find the resonance frequencies of this vowel?
    - The length of the tube (vocal tract)
    - The boundary conditions of the tube
    - The speed of sound in air (use 350 m/s)

## 4. Deriving the vocal-tract filter for [ə]

- We know how to calculate the resonance frequencies for a tube of this type: it is a **node/antinode** or **quarter-wavelength** system
  - What is the distance between each pair of resonance frequencies in a system of this type?



## 4. Deriving the vocal-tract filter for [ə]

- We know how to calculate the resonance frequencies for a tube of this type: it is a **node/antinode** or **quarter-wavelength** system
  - What is the distance between each pair of resonance frequencies in a system of this type?
    - Each resonance is an odd-numbered multiple of the first ( $1*f_1, 3*f_1, 5*f_1, \dots$ )
    - So the distance between each pair of resonances is  $2\times$  the lowest resonance's frequency

## 4. Deriving the vocal-tract filter for [ə]

- The **precise values** for the formants of [ə], or any vowel, will differ from person to person, since people have vocal tracts of different lengths
  - However, the **relative distance between** the formants for each vowel in a language is (reasonably) consistent from speaker to speaker

## 4. Deriving the vocal-tract filter for [ə]

- For a vocal tract that is 17.5 cm (0.175 m) long, calculate the first three resonance frequencies
  - These values are the **first three formants** of [ə] for this vocal tract (use “F” for formant frequencies)

## 4. Deriving the vocal-tract filter for [ə]

- For a vocal tract that is 17.5cm (0.175m) long, calculate the first three resonance frequencies
  - These values are the **first three formants** of [ə] for this vocal tract (use “F” for formant frequencies)

1st resonance frequency ( $F_1$ ):

$$F_1 = c/\lambda_1 \quad \lambda_1 = 4L = 4*0.175\text{m} = 0.70\text{m}$$
$$c = 350\text{m/s}$$

$$F_1 = (350\text{m/s})/(0.70\text{m}) = 500/\text{s} = \mathbf{500\text{Hz}}$$

$F_2$  and  $F_3$  are odd-numbered multiples of  $F_1$ :

$$F_2 = 3*500\text{Hz} = \mathbf{1500\text{Hz}} \quad | \quad F_3 = 5*500\text{Hz} = \mathbf{2500\text{Hz}}$$

## 5. Putting source and filter together: [ə]

- Synthesized [ə] [[vs x.wav](#)] (using same glottal source)  
(U Delaware Speech Research Tutorials)
  - Open this sound file in Praat
  - View the **waveform**
  - View the **spectrum** (window length=0.5 sec)
- Understanding this [ə] spectrum:
  - What determines the components' **frequencies**?
  - What determines their **amplitudes**?

## 5. Putting source and filter together: [ə]

- Will [ə] produced by someone with a 17.5cm vocal tract always have **components** at 500Hz, 1500Hz, and 2500Hz?

## 5. Putting source and filter together: [ə]

- Will [ə] produced by someone with a 17.5cm vocal tract always have **components** at 500Hz, 1500Hz, and 2500Hz?

**NO!**

## 5. Putting source and filter together: [ə]

- **VERY IMPORTANT**
  - The vocal-tract **filter** is not a sound **source**
  - The filter is not adding components to the complex wave at its own resonance frequencies
  - All component **frequencies** in the source-filter model are coming from the **source**
  - The **filter's** job is only to modify **amplitudes** of the components contributed by the source



## 5. Putting source and filter together: [ə]

- For next time:

See web demo "[The source/filter model](#)"

(Kevin Russell, U. Manitoba)

- The **filter** associated with [ə] (for a vocal tract of a particular length)
- The **spectrum** of the **glottal source** (for voicing produced with a particular  $f_0$ )
- The **spectrum** of the **resulting [ə]**—which is the result of **modifying** the given glottal source with the given [ə] filter

## 5. Putting source and filter together: [ə]

- When we put source and filter together...
  - In the spectrum of the [ə], the **components** (also called *harmonics*) of the **source** wave near the **formants** (the frequencies corresponding to amplitude peaks in the **filter**) are **amplified** the most
  - Note that the amplification effect falls off gradually from a peak; this peak marks the actual formant/resonance frequency

## 5. Putting source and filter together: [ə]

- When we put source and filter together...
  - The **frequencies** of the components of the resulting sound are determined by the \_\_\_\_\_
  - The **amplitudes** of the components of the resulting sound are determined by the \_\_\_\_\_

## 5. Putting source and filter together: [ə]

- When we put source and filter together...
  - The **frequencies** of the components of the resulting sound are determined by the **source**
  - The **amplitudes** of the components of the resulting sound are determined by the **filter**

## 5. Putting source and filter together: [ə]

- ALWAYS REMEMBER:

**Formants** are related to **vocal-tract** size and shape, **NOT** to  $f_0$  of phonation!

(a) The same vowel can be sung on different pitches

(b) Different vowel categories can be sung on the same pitch

- If the glottal source determined the formant frequencies, or vice-versa,

**(a) and (b) would be impossible**

## 6. Terms and abbreviations for frequencies

When we are talking about **speech acoustics**:

- The abbreviation  $f_0$  (or F0,  $F_0$ ) is used for the **fundamental frequency** of the **glottal source**
- The abbreviation **H(n)** is often used for the  $n$ th **resonance** ( $n$ th "harmonic"=whole-number multiple) of the **glottal source**
  - The glottal source has components at whole number multiples of the lowest resonance, so the lowest resonance =  $f_0$  (remember GCD?)
  - Thus, for a voiced speech sound,  $f_0 = H1$

## 6. Terms and abbreviations for frequencies

When we are talking about **speech acoustics**:

- The abbreviation **F1** is used for the **first formant**, that is, the **first resonance frequency** of the vocal-tract **filter**
- **F2, F3**, etc. are used for the 2nd, 3rd, etc, **formants**, that is, **subsequent resonance frequencies** of the vocal-tract **filter**
- *Comprehension check*: What is the relationship between  $f_0$  (F0) and F1 in a vowel?

## 6. Terms and abbreviations for frequencies

When we are talking about waves **in general**:

- $f_0$  (sometimes  $F_0$ ,  $F_0$ ) is used for the **fundamental frequency** of any wave, simple or complex
- $f_n$  is used for the  $n$ th resonance frequency of a standing-wave system

So:

- *IF* the object under analysis is a sound **source**,
- and *IF* higher resonances are all some **multiple** of the first one,

$$\text{THEN } f_0 = f_1$$