

- **The source-filter model of vowel acoustics**
- **Modeling schwa**

Background reading:

- *AAP Ch 2, sec 2.1 and 2.4 (review)*

0. Today's objectives

After today's class, you should be able to:

- **Explain**, and **calculate**, how the **frequencies** and the (relative) **amplitudes** of the components are determined for a uniform-vocal-tract [ə] in the **source-filter model of vowel acoustics**
 - The contribution of the glottal source
 - The contribution of the vocal-tract filter
- Recognize and correctly use terms and abbreviations for frequencies in different contexts

1. Review: Tube resonances

- Last week in class:

How do we get from tube length to resonance frequencies?

- Lab #3:

How do we get from resonance frequencies to tube length?

1. Review: Tube resonances

- Last week in class:

How do we get from tube length to resonance frequencies? $L \rightarrow \lambda_n \rightarrow f_n$, for the n^{th} resonance

- Lab #3:

How do we get from resonance frequencies to tube length? $f_n \rightarrow \lambda_n \rightarrow L$, for the n^{th} resonance

2. The glottal-source wave

- Review: What is the **glottal-source wave**?
 - Also called the **voicing wave**(form) in *AAP* Ch 2
 - The sound wave produced by _____

2. The glottal-source wave

- Review: What is the **glottal-source wave**?
 - Also called the **voicing wave**(form) in *AAP* Ch 2
 - The sound wave produced by the vibration of the vocal folds
- To actually hear this sound wave, you would have to put a microphone right above the glottis
 - The sound waves of any speech we normally hear are **further modified** by passing through the vocal tract
 - That is the **filter** part of the source/filter model!

2. The glottal-source wave

- The **shape** of this wave is determined by the way the vocal folds open quickly and close gradually
→ More about this later in the semester
- Computer-synthesized glottal-source wave:
[[lsrc.wav](#)] (U Delaware Speech Research Tutorials)
- Look at the **waveform** in Praat
 - Periodic? Simple or complex? What is f_0 ?

2. The glottal-source wave

- Computer-synthesized glottal-source wave:
[[lsrc.wav](#)] (U Delaware Speech Research Tutorials)
- Look at the **waveform** in Praat
 - Periodic? Simple or complex? What is f_0 ?
- Look at the **spectrum** (window length = 0.5 sec)
 - What is the lowest-frequency component?
 - How do the components' **frequencies** relate?
 - How do the components' **amplitudes** relate?
 - What is f_0 ? (should get the same answer as above!)

2. The glottal-source wave

- Characteristics of the glottal-source wave
 - **Amplitudes** of the components gradually **decrease** (assuming modal or 'ordinary' voicing)
 - **Frequencies** of the components are **whole-number multiples** of the lowest component
- The component frequencies thus have the *same relationship* as in a node/node system
 - Careful here: The vocal folds do not actually vibrate like a string of fixed length (they open and close to emit puffs of air)

2. The glottal-source wave

- Can the **frequencies** of the **components** of the glottal-source wave be manipulated by the speaker?

2. The glottal-source wave

- Can the **frequencies** of the **components** of the glottal-source wave be manipulated by the speaker?

Yes!

- Each human's voice can produce a range of f_0 values (or else singing would be impossible)
- Manipulating f_0 means manipulating the component frequencies
 - f_0 is the GCD of the component frequencies
 - So in the glottal-source wave, f_0 is the same as the first component frequency

2. The glottal-source wave

- If someone produces a vowel with $f_0 = 250 \text{ Hz}$, what are the frequencies of the **first five components** of the **glottal-source wave**?

2. The glottal-source wave

- If someone produces a vowel with $f_0 = 250$ Hz, what are the frequencies of the **first five components** of the **glottal-source wave**?
 - f_1 (H1) = $f_0 = 250$ Hz | *don't forget the first one!*
 - f_2 (H2) = $2 * f_1 = 500$ Hz | *whole-number multiples*
 - f_3 (H3) = $3 * f_1 = 750$ Hz
 - f_4 (H4) = $4 * f_1 = 1000$ Hz
 - f_5 (H5) = $5 * f_1 = 1250$ Hz
- The components of the glottal-source wave are often called **harmonics**, abbreviated **H(n)**

3. Overview of the source-filter model

- How do you get a trumpet to play a note?

3. Overview of the source-filter model

- To play a trumpet, you “buzz” your lips
 - This creates a **sound source** at one end of the trumpet (disturbance in the medium!)
- But what we *hear* is a trumpet note, not a buzz:
The trumpet acts as a **filter**
 - It **changes the shape** (→ the **sound quality**) of the **complex wave** produced by the sound source
 - It does this by **suppressing** (reducing the amplitude of) some of the source wave’s **components** and **amplifying** (increasing the amplitude of) others

3. Overview of the source-filter model

- In much the same way, when we produce a **voiced speech sound** such as a **vowel**...
 - The vocal folds **buzz** (glottal-source wave)
 - The vocal-tract tube **changes the shape** of the complex wave by **suppressing** some source **components** and **amplifying** others
- The **source-filter model** of the vocal tract
 - Sound **source**: the **vibrating vocal folds**
 - **Filter**: the vocal tract as a **tube** (or a series of tubes)

4. The vocal-tract filter

- Much like a trumpet, the vocal tract **filters** the sound energy by **suppressing** some **components** of the glottal-source wave and **amplifying** others
 - The components **amplified** by the vocal tract are those close to its **resonance frequencies**
 - The **resonance frequencies** of the vocal tract depend on its **length** and **shape**
 - The vocal tract forms different **shapes** for different **vowels** (and consonants—more on this later)
- Therefore, each different **vowel** (such as [i] vs. [a]) corresponds to a different vocal-tract **filter**

4. The vocal-tract filter

- So if each different **vowel** corresponds to a different vocal-tract **filter** ...

This means that each **vowel** corresponds to a different set of **amplified frequencies** (vocal-tract **resonances**)

- **These are known as the vowel's formants**

4. The vocal-tract filter

- Try it out: Synthesized vowels [[lii.wav](#)] | [[laa.wav](#)]
(U Delaware Speech Research Tutorials)
- Download and open these sound files in Praat
 - What **vowels** are they? (What do you hear?)
 - Compare them to each other and to the glottal-source wave we looked at before [[lsrc.wav](#)]:
 - How do their **f_0 s** compare?
 - How do their waveform **shapes** compare?
 - How do their **spectra** compare?

4. The vocal-tract filter

- Each vowel (such as [i] vs. [a]) corresponds to a different set of **resonance frequencies (formants)**
- The **shape of a complex wave** is determined by the frequencies **and amplitudes** of its components
 - Two different vowel categories have **differently shaped** sound waves *even when they are sung on the same pitch* (=have the same glottal-source wave)
- Waves of different shapes correspond to sounds with different **sound qualities (timbres)** — this is how different vowels differ perceptually

5. Deriving the vocal-tract filter for [ə]

- To analyze the acoustics of vowels, we need to understand **why** they have the resonance frequencies (formants) that they have
- The first step: What are the resonance frequencies of the **neutral vocal-tract vowel, [ə]**?
 - The vocal tract is approximately a **uniform tube** that is **closed** at one end (the glottis) and **open** at the other end (the lips)
 - The neutral vocal-tract vowel is typically represented as [ə] (schwa), but note that it doesn't sound exactly the same as English [ə] as in *sofa*

5. Deriving the vocal-tract filter for [ə]

- The first step: What are the resonance frequencies of the **neutral vocal-tract vowel, [ə]**?
 - The vocal tract is approximately a **uniform tube** that is **closed** at one end (the glottis) and **open** at the other end (the lips)
 - What do we need to know in order to find the resonance frequencies of this vowel?

5. Deriving the vocal-tract filter for [ə]

- The first step: What are the resonance frequencies of the **neutral vocal-tract vowel, [ə]**?
 - The vocal tract is approximately a **uniform tube** that is **closed** at one end (the glottis) and **open** at the other end (the lips)
 - What do we need to know in order to find the resonance frequencies of this vowel?
 - The length of the tube (vocal tract)
 - The boundary conditions of the tube
 - The speed of sound in air (use 350 m/s)

5. Deriving the vocal-tract filter for [ə]

- We know how to calculate the resonance frequencies for a tube of this type: it is a **node/antinode** or **quarter-wavelength** system
 - What is the distance between each pair of resonance frequencies in a system of this type?

5. Deriving the vocal-tract filter for [ə]

- We know how to calculate the resonance frequencies for a tube of this type: it is a **node/antinode** or **quarter-wavelength** system
 - What is the distance between each pair of resonance frequencies in a system of this type?
 - Each resonance is an odd-numbered multiple of the first ($1*f_1, 3*f_1, 5*f_1, \dots$)
 - So the distance between each pair of resonances is $2\times$ the lowest resonance's frequency

5. Deriving the vocal-tract filter for [ə]

- The **precise values** for the formants of [ə], or any vowel, will differ from person to person, since people have vocal tracts of different lengths
 - However, the **relative distance between** the formants for each vowel in a language is (reasonably) consistent from speaker to speaker

5. Deriving the vocal-tract filter for [ə]

- For a vocal tract that is 17.5 cm (0.175 m) long, calculate the first three resonance frequencies
 - These values are the **first three formants** of [ə] for this vocal tract (use “F” for formant frequencies)

5. Deriving the vocal-tract filter for [ə]

- For a vocal tract that is 17.5cm (0.175m) long, calculate the first three resonance frequencies
 - These values are the **first three formants** of [ə] for this vocal tract (use “F” for formant frequencies)

1st resonance frequency (F_1):

$$F_1 = c/\lambda_1 \qquad \lambda_1 = 4L = 4*0.175\text{m} = 0.70\text{m}$$

$$c = 350\text{m/s}$$

$$F_1 = (350\text{m/s})/(0.70\text{m}) = 500/\text{s} = \mathbf{500\text{Hz}}$$

F_2 and F_3 are odd-numbered multiples of F_1 :

$$F_2 = 3*500\text{Hz} = \mathbf{1500\text{Hz}} \mid F_3 = 5*500\text{Hz} = \mathbf{2500\text{Hz}}$$

6. Putting source and filter together: [ə]

- Synthesized [ə] [[vs x.wav](#)] (using same glottal source)
(U Delaware Speech Research Tutorials)
 - Open this sound file in Praat
 - View the **waveform**
 - View the **spectrum** (window length=0.5 sec)
- Understanding this [ə] spectrum:
 - What determines the components' **frequencies**?
 - What determines their **amplitudes**?

6. Putting source and filter together: [ə]

Discussion

- Will [ə] produced by someone with a 17.5cm vocal tract always have **components** at 500Hz, 1500Hz, and 2500Hz?

6. Putting source and filter together: [ə]

- Will [ə] produced by someone with a 17.5cm vocal tract always have **components** at 500Hz, 1500Hz, and 2500Hz?

NO!

6. Putting source and filter together: [ə]

- **VERY IMPORTANT**

- The vocal-tract **filter** is not a sound **source**
- The filter is not adding components to the complex wave at its own resonance frequencies
- All component **frequencies** in the source-filter model are coming from the **source**
- The **filter**'s job is only to modify **amplitudes** of the components contributed by the source

6. Putting source and filter together: [ə]

- For next time:

See web demo “[The source/filter model](#)”

(Kevin Russell, U. Manitoba)

- The **filter** associated with [ə] (for a vocal tract of a particular length)
- The **spectrum** of the **glottal source** (for voicing produced with a particular f_0)
- The **spectrum** of the **resulting [ə]**—which is the result of **modifying** the given glottal source with the given [ə] filter

6. Putting source and filter together: [ə]

- When we put source and filter together...
 - In the spectrum of the [ə], the **components** (also called *harmonics*) of the **source** wave near the **formants** (the frequencies corresponding to amplitude peaks in the **filter**) are **amplified** the most
 - Note that the amplification effect falls off gradually from a peak; this peak marks the actual formant/resonance frequency

6. Putting source and filter together: [ə]

- When we put source and filter together...
 - The **frequencies** of the components of the resulting sound are determined by the _____
 - The **amplitudes** of the components of the resulting sound are determined by the _____

6. Putting source and filter together: [ə]

- When we put source and filter together...
 - The **frequencies** of the components of the resulting sound are determined by the **source**
 - The **amplitudes** of the components of the resulting sound are determined by the **filter**

6. Putting source and filter together: [ə]

- ALWAYS REMEMBER:

Formants are related to **vocal-tract** size and shape, **NOT** to f_0 of phonation!

- (a) The same vowel can be sung on different pitches
- (b) Different vowel categories can be sung on the same pitch
- If the glottal source determined the formant frequencies, or vice-versa,
(a) and (b) would be impossible

7. Terms and abbreviations for frequencies

When we are talking about **speech acoustics**:

- The abbreviation **f_0** (or F0, F_0) is used for the **fundamental frequency** of the **glottal source**
- The abbreviation **H(n)** is often used for the n th **resonance** (n th "**harmonic**"=whole-number multiple) of the **glottal source**
 - The glottal source has components at whole number multiples of the lowest resonance, so the lowest resonance = f_0 (remember GCD?)
 - Thus, for a voiced speech sound, **$f_0 = H1$**

7. Terms and abbreviations for frequencies

When we are talking about **speech acoustics**:

- The abbreviation **F1** is used for the **first formant**, that is, the **first resonance frequency** of the vocal-tract **filter**
- **F2, F3**, etc. are used for the 2nd, 3rd, etc, **formants**, that is, **subsequent resonance frequencies** of the vocal-tract **filter**
- *Comprehension check*: What is the relationship between f_0 (F0) and F1 in a vowel?

7. Terms and abbreviations for frequencies

When we are talking about waves **in general**:

- f_0 (sometimes F_0 , F_0) is used for the **fundamental frequency** of any wave, simple or complex
- f_n is used for the n th resonance frequency of a standing-wave system

So:

- *IF* the object under analysis is a sound **source**,
- and *IF* higher resonances are all some **multiple** of the first one,

$$\text{THEN } f_0 = f_1$$